

# A Theoretical Study of $^{31}\text{P}$ and $^{95}\text{Mo}$ NMR Chemical Shifts in $\text{M}(\text{CO})_5\text{PR}_3$ ( $\text{M} = \text{Cr}, \text{Mo}$ ; $\text{R} = \text{H}, \text{CH}_3, \text{C}_6\text{H}_5, \text{F}, \text{and Cl}$ ) Based on Density Functional Theory and Gauge-Including Atomic Orbitals

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Received: October 13, 1997; In Final Form: January 5, 1998

A theoretical study has been carried out on  $^{31}\text{P}$  NMR chemical shifts in the phosphine-substituted metal carbonyls of the type  $\text{M}(\text{CO})_5\text{PR}_3$  ( $\text{M} = \text{Cr}$  and  $\text{Mo}$ ;  $\text{R} = \text{H}, \text{CH}_3, \text{C}_6\text{H}_5, \text{F}, \text{and Cl}$ ) as well as the  $^{95}\text{Mo}$  NMR chemical shift of  $\text{Mo}(\text{CO})_5\text{P}(\text{C}_6\text{H}_5)_3$  and  $\text{Mo}(\text{CO})_5\text{PX}_3$  ( $\text{X} = \text{F}$  and  $\text{Cl}$ ). The study was based on density functional theory (DFT) and gauge-including atomic orbitals (GIAO). The calculated chemical shifts and the components of the chemical shift tensor are in good agreement with the available experimental data. The coordination chemical shift expressed as the difference in the isotropic shifts  $\Delta\delta = \delta_{\text{M}(\text{CO})_5\text{PR}_3} - \delta_{\text{PR}_3}$  between  $\text{PR}_3$  as a ligand,  $\delta_{\text{M}(\text{CO})_5\text{PR}_3}$ , and free  $\text{PR}_3$ , was analyzed in detail. It was shown that the paramagnetic coupling between the  $\pi$  orbitals of the complexed  $\text{PR}_3$  ligand  $\pi_{\text{PR}_3}$  and the  $d_\sigma$  metal-based LUMO of the  $\text{M}(\text{CO})_5\text{PR}_3$  complex has a positive contribution to the coordination chemical shift,  $\Delta\delta$ , whereas the paramagnetic couplings between  $\sigma_{\text{PR}_3}$  and  $\pi^*_{\text{PR}_3}$  as well as  $\pi_{\text{PR}_3}$  and  $\pi^*_{\text{PR}_3}$  of the complexed ligand have a negative contributions to  $\Delta\delta$  for  $\text{PF}_3$  and  $\text{PCl}_3$ . It is the latter type of couplings that are responsible for the total negative coordination shift in the case of  $\text{PCl}_3$ . The calculated  $^{95}\text{Mo}$  NMR chemical shifts of  $\text{Mo}(\text{CO})_5\text{P}(\text{C}_6\text{H}_5)_3$  and  $\text{Mo}(\text{CO})_5\text{PX}_3$  ( $\text{X} = \text{F}$  and  $\text{Cl}$ ) are in good agreement with experiment. The major contribution comes from the paramagnetic coupling between the occupied  $d_\pi$  orbitals (HOMO) and the virtual  $d_\sigma$  orbitals (LUMO).

## 1. Introduction

It has in the past decade become possible to carry out calculations on NMR chemical shifts<sup>1–4</sup> with increasing accuracy. In this regard, the application of density functional theory (DFT) has been especially useful for compounds containing heavy elements. The use of DFT in NMR calculations has been pioneered by Malkin<sup>5</sup> within the “individual gauge for localized orbitals” approach (IGLO)<sup>3a</sup> and subsequently applied by Kaupp<sup>6</sup> and Bühl.<sup>7d,e</sup> Schreckenbach<sup>8a,b</sup> and Ziegler have more recently presented in a method in which the NMR shielding tensor is calculated by combining the “gauge-including atomic orbitals” (GIAO) approach<sup>9a,b</sup> with density functional theory (DFT) following earlier work by Seifert<sup>9c,d</sup> et al. A number of applications<sup>10</sup> have shown that the GIAO-DFT scheme is capable of reproducing experimental values for ligand chemical shifts of transition metal complexes<sup>10a,b,e</sup> and chemical shifts of heavy main group elements.<sup>10c,d</sup> The DFT-GIAO scheme has further been extended to include the frozen core approximation<sup>11a</sup> and the scalar relativistic two-component Pauli type Hamiltonian<sup>11b</sup> for relativistic calculations. The DFT-GIAO implementation makes full use of the modern features of DFT in terms of accurate exchange–correlation (XC) energy functionals and large basis sets. The DFT-GIAO method has also been implemented by Rauhut<sup>8c</sup> et al. and Cheeseman<sup>8d</sup> et al. as well as Handy<sup>8e</sup> et al. The DFT-GIAO method has further been used in conjunction with hybrid DFT methods<sup>12b</sup> by Bühl<sup>7a–c</sup> as well as Godbout and Oldfield.<sup>12a</sup> Traditional ab initio methods have also been applied by Nakatsuji<sup>3c,13</sup> et al. to the calculation of NMR chemical shifts in compounds containing heavy elements.

We present calculations on the  $^{31}\text{P}$  chemical shift and chemical shift components for  $\text{M}(\text{CO})_5\text{PR}_3$  ( $\text{M} = \text{Cr}$  and  $\text{Mo}$ ;

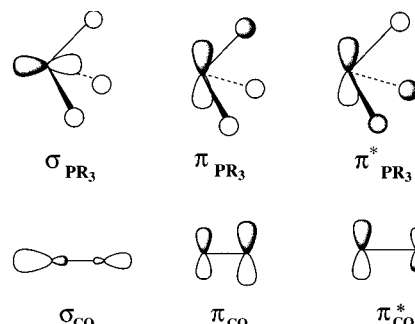


Figure 1. Frontier orbitals in  $\text{PR}_3$  and  $\text{CO}$ .

$\text{R} = \text{H}, \text{CH}_3, \text{C}_6\text{H}_5, \text{F}, \text{and Cl}$ ) as well as the  $^{95}\text{Mo}$  NMR chemical shift of  $\text{Mo}(\text{CO})_5\text{P}(\text{C}_6\text{H}_5)_3$  and  $\text{Mo}(\text{CO})_5\text{PX}_3$  ( $\text{X} = \text{F}$  and  $\text{Cl}$ ) based on the GIAO-DFT approach.<sup>8a,b,11</sup> One objective of our study has been to test the accuracy and predictive power of the GIAO-DFT method by comparing theoretical results to the well-established experimental values and results from other theoretical methods. We shall in addition try to explain how the  $^{31}\text{P}$  chemical shift of  $\text{PR}_3$  is changed as the molecule is complexed to a metal center. A comparison will also be made to our recent DFT-GIAO<sup>10a,e</sup> studies on binary carbonyl complexes in which the difference (coordination shift) in the isotropic shielding  $\Delta\delta = \sigma_{\text{CO}} - \sigma_{\text{M}(\text{CO})_n}$  between free  $\text{CO}$  and  $\text{CO}$  as a ligand,  $\sigma_{\text{M}(\text{CO})_n}$  was analyzed in detail. Phosphine is similar (isolobal) to  $\text{CO}$  as a ligand in that both molecules contain a  $\sigma$ -type orbital, two  $\pi$ -type orbitals and two  $\pi^*$ -type orbitals, see Figure 1.

Kaupp<sup>6f</sup> was the first to carry out DFT calculations on the  $^{31}\text{P}$  coordination shifts ( $\Delta\delta$ ) in a study on  $\text{M}(\text{CO})_5\text{L}$  [ $\text{M} = \text{Cr}, \text{Mo}, \text{and W}$ ;  $\text{L} = \text{PH}_3, \text{P}(\text{CH}_3)_3, \text{PF}_3, \text{and PCl}_3$ ] by using the sum-over-states density-functional perturbation theory (SOS-

DFPT) by Malkin<sup>5a-c</sup> et al. His analysis of <sup>31</sup>P shielding tensors in the free ligands in terms of canonical molecular orbitals is comparable with our findings. However, a detailed analysis of the computed trends in the metal complexes in terms of individual electronic excitations was not possible. Here, we have been able to analyze the observed coordination chemical shifts in terms of specific paramagnetic couplings between occupied and virtual orbitals. Some recent experimental solid-state <sup>31</sup>P studies on Cr(CO)<sub>5</sub>Ph<sub>3</sub> and Cr(CO)<sub>4</sub>(CS)Ph<sub>3</sub> makes it further possible for the first time to compare observed and calculated shift tensor components in phosphine complexes and test the DFT-GIAO method for this type of large size systems.

Wasylishen et al.<sup>14a-d</sup> have pioneered the recording of <sup>31</sup>P and <sup>95</sup>Mo NMR shifts in the solid state. The interpretation of <sup>31</sup>P phosphine coordination shifts in terms of the σ-donor and π-acceptor abilities of these ligands has been pioneered by Alyea<sup>15</sup> et al. on the basis of a number of careful experimental investigations involving Mo(CO)<sub>5</sub>PR<sub>3</sub> complexes. Alyea<sup>15</sup> et al. have further included <sup>95</sup>Mo NMR in their investigation. We shall here extend our NMR shift calculations to <sup>95</sup>Mo. The field of <sup>95</sup>Mo has been reviewed by Malito.<sup>14e</sup>

## 2. Computational Details and the GIAO-DFT Method

Our implementation of the DFT-GIAO method has been described in details elsewhere.<sup>8a-b,10</sup> It is based on the Amsterdam density functional package ADF.<sup>6-21</sup> We use experimental geometries, unless otherwise stated. The exchange–correlation (XC) energy functional according to Becke<sup>22</sup> and Perdew<sup>23</sup> are employed self-consistently on top of the local density approximation (LDA).

We employ an uncontracted triple-ζ quality valence basis of Slater type atomic orbitals (STOs).<sup>24</sup> The valence region of the basis is extended by two sets of d (p for hydrogen) polarization functions per atomic center.

The metal center was described by an uncontracted triple-ζ STO basis set<sup>24,25</sup> for the outer *ns*, *np*, *nd*, (*n*+1)*s*, and (*n*+1)*p* orbitals extended by two sets of d polarization functions, whereas the shells of lower energy were treated by the frozen core approximation.<sup>11a,16</sup> The valence on phosphorus included the 1s shell and was described by an uncontracted triple-ζ STO basis augmented by two 3d and one 4f function, corresponding to basis set V of the ADF package.<sup>21</sup> A set of auxiliary<sup>26</sup> s, p, d, f, and g STO functions, centered on all nuclei, was used in order to fit the molecular density and present Coulomb and exchange potentials accurately in each SCF cycle.

The NMR shielding tensor for nucleus N can be written as<sup>8a</sup>

$$\sigma_{\lambda\nu} = \sigma_{\lambda\nu}^d + \sigma_{\lambda\nu}^p = \int \frac{\vec{r}_N \times [\vec{J}_v^d(\vec{r}_N) + \vec{J}_v^p(\vec{r}_N)]_\lambda}{r_N^3} d\vec{r}_N \quad (1)$$

Here  $\vec{J}^d$  and  $\vec{J}^p$  are respectively the diamagnetic and paramagnetic current densities<sup>8a</sup> induced by an external magnetic field  $\vec{B}_0$ . Equation 1 involves an expectation value of  $r_N^{-3}$  where  $r_N$  is the distance to the NMR nucleus. The paramagnetic current density originates primarily from a coupling between occupied  $\Psi_i$  and virtual orbitals  $\Psi_a$ , induced by the external magnetic field  $\vec{B}_0$ .

$$\vec{J}^p = \sum_{s=1}^3 \sum_i^{\text{occ}} \sum_a^{\text{uocc}} u_{ai}^{(1,s)} [\Psi_i \vec{\nabla} \Psi_a - \Psi_a \vec{\nabla} \Psi_i] B_{0s} \quad (2)$$

The principle contribution to the coupling  $u_{ai}^{(1)}$  is given by

$$u_{ai}^{(1)} \approx \infty - \frac{1}{2(\epsilon_i^{(0)} - \epsilon_a^{(0)})} \sum_{\lambda,\nu} c_{\lambda a}^{(0)} c_{\nu i}^{(0)} \{ \langle \chi_\lambda | [\vec{r}_v \times \vec{\nabla}]_u | \chi_\nu \rangle \} \\ \propto - \frac{1}{2(\epsilon_i^{(0)} - \epsilon_a^{(0)})} \langle \Psi_a | \hat{M}_u | \Psi_i \rangle \quad (3)$$

Here  $\epsilon^{(0)}$  refers to orbital energies of the unperturbed molecules without the external magnetic field.  $\langle \Psi_a | \hat{M}_u | \Psi_i \rangle$  represents the first-order magnetic coupling between an occupied molecular orbital, *i*, and a virtual orbital, *a*. Within the GIAO formalism,<sup>8a</sup> the action of the magnetic operator  $\hat{M}_u$  on  $\Psi_q$  is simply to work with  $i\hat{L}_u^v$  on each atomic orbital  $x_v$ . Here  $\hat{L}_u^v$  is the *u*-component of the angular momentum operator with its origin at the center  $\vec{R}_v$  on which  $x_v$  is situated. Tabulations for  $\hat{L}_u^v x_v$  are available in the literature.<sup>27,28</sup>

## 3. Results and Discussions

We shall now provide a discussion of how the <sup>31</sup>P shift tensor in PR<sub>3</sub> is modified as the PR<sub>3</sub> molecule is complexed to a metal center. The discussion will start with the free PR<sub>3</sub> ligand and continue to (CO)<sub>5</sub>MPR<sub>3</sub> in the following sections. The coordinate systems are always chosen such that the z-axis points along the C<sub>3</sub>-axis in the free ligand or the M–P bond vector in the (CO)<sub>5</sub>MPR<sub>3</sub> complexes. The x-axis is placed in the C<sub>s</sub> reflexion plane of the (CO)<sub>5</sub>MPR<sub>3</sub> complex.

The chemical shift of a sample nuclei relative to a reference can be written with sufficient accuracy for our purpose as<sup>29a</sup>

$$\delta_{\text{sample}} = \sigma_{\text{reference}} - \sigma_{\text{sample}} \quad (4a)$$

Complexation of a ligand to a metal is accompanied by changes in the chemical shifts of the ligand atoms. These effects are usually analyzed in terms of the coordination chemical shift. The coordination shift is defined as<sup>29b</sup>

$$\Delta\delta = \delta_{\text{complex}} - \delta_{\text{ligand}} \quad (4b)$$

In our discussion the shielding terminology ( $\sigma$ ) will be employed as well. Given the opposite signs of  $\sigma$  (shielding) and  $\delta$  (chemical shift), the coordination shift should be defined in terms of the shielding terminology as

$$\Delta\delta = \sigma_{\text{ligand}} - \sigma_{\text{complex}} \quad (4c)$$

Thus, the coordination shift is defined as the difference in the shielding of the free ligand and the shielding of the ligand in the complex.

## 4. Free PR<sub>3</sub>

The <sup>31</sup>P NMR paramagnetic, diamagnetic, and isotropic components of the chemical shielding tensor for the free phosphines are presented in Table 1 together with the available experimental data. Experimental structures idealized to C<sub>3v</sub> symmetry have been used in all calculations on the free PR<sub>3</sub> molecule. The components of the shielding tensors perpendicular and parallel to the C<sub>3</sub> axis are given as  $\sigma_\perp$  and  $\sigma_\parallel$ , respectively. There is a good agreement between theory and experiment for PH<sub>3</sub>, P(CH<sub>3</sub>)<sub>3</sub>, and P(C<sub>6</sub>H<sub>5</sub>)<sub>3</sub> with deviations of 15 ppm. The agreement is less satisfactory for PF<sub>3</sub> and PCl<sub>3</sub> with deviations up to 60 ppm.

The total shielding components  $\sigma_\perp$  and  $\sigma_\parallel$  are dominated by large positive diamagnetic contributions  $\sigma_\perp^d$  and  $\sigma_\parallel^d$  whereas the paramagnetic components  $\sigma_\perp^p$  and  $\sigma_\parallel^p$  are negative, and in most

**TABLE 1: Experimental and Calculated Shielding Tensors<sup>a</sup> for Free Phosphines<sup>a</sup>**

molecule	$\sigma_{\perp}^d$	$\sigma_{\perp}^p$	$\sigma_{\perp}$	$\sigma_{\parallel}^d$	$\sigma_{\parallel}^p$	$\sigma_{\parallel}$	$\sigma$
PH <sub>3</sub>	965.4 (981.5) <sup>b</sup>	-372.2 (-368.4) <sup>b</sup>	593.2 (613.1) <sup>b</sup>	963.5 (980.0) <sup>b</sup>	-439.4 (-422.9) <sup>b</sup>	524.1 (557.1) <sup>b</sup>	570.2 (594.4) <sup>b</sup>
P(CH <sub>3</sub> ) <sub>3</sub>	958.3	-559.7	398.6 (389.2) <sup>b</sup>	946.6	-586.0	360.6 (396.8) <sup>b</sup>	385.9 (391.7) <sup>b</sup>
PPh <sub>3</sub>	959.5	-645.9	313.6 (319.3) <sup>c,d</sup>	953.6	-618.9	334.7 (370.3) <sup>c,d</sup>	320.6 (336.3) <sup>c,d</sup>
PF <sub>3</sub>	948.5	-857.2	91.3 (162.4) <sup>b</sup>	938.8	-583.9	354.9 (343.4) <sup>b</sup>	179.2 (222.7) <sup>b</sup>
PCl <sub>3</sub>	966.9	-971.8	-4.9	958.6	-811.5	147.1	45.8 (111.3) <sup>b</sup>

<sup>a</sup> All numbers are in ppm. The component  $\sigma_{\perp}$  is perpendicular to  $C_{3v}$  axis,  $\sigma_{\parallel}$  is parallel to  $C_3$  axis. Superscripts p and d indicate paramagnetic and diamagnetic components, respectively. <sup>b</sup> Experimental numbers from ref 45. <sup>c</sup> Experimental numbers from ref 40. <sup>d</sup> Experimental numbers are in parentheses. Experimental data originally reported as chemical shift ( $\delta$ ) were converted to absolute shielding ( $\sigma$ ) using the experimental data <sup>31</sup>P in 85% H<sub>3</sub>PO<sub>4</sub> (aq)  $\sigma_{\text{H}_3\text{PO}_4} = 328.35$  ppm (ref 45) and  $\delta = \sigma_{\text{H}_3\text{PO}_4} - \sigma_{\text{substance}}$ .

**TABLE 2: Calculated and Experimental <sup>31</sup>P Chemical Shift Tensor Components and Isotropic Chemical Shift for Free PR<sub>3</sub> and M(CO)<sub>5</sub>PR<sub>3</sub> (Values in ppm) Comparison with <sup>13</sup>C for Free CO and Cr(CO)<sub>6</sub>**

system	cone angle	$\delta_{xx}^y$	$\delta_{yy}^y$	$\delta_{zz}^y$	$\delta^d$	$\delta^p$	chemical shift $\delta$ (exptl) <sup>r</sup>
CO <sup>c</sup>		328.9 (317.7) <sup>r</sup>	328.9 (317.7)	-94.1 (-88.0)	-4.6	192.5	187.9(184.4)
Cr(CO) <sub>6</sub> <sup>c</sup>		354.0 (353.0)	354.0 (353.0)	-86.3 (-70.0)	-12.1	219.3	207.2 (212.0)
PH <sub>3</sub> <sup>f</sup>	87.0 <sup>j</sup>	-277.7 (-284.8) <sup>s</sup>	-277.7 (-284.8) <sup>s</sup>	-208.6 (-228.8) <sup>s</sup>	-9.1	-245.6	-254.7 <sup>a</sup> (-266.1) <sup>s</sup>
Cr(CO) <sub>5</sub> PH <sub>3</sub> <sup>g</sup>		-67.5	-67.5	-211.1	-12.5	-102.9	-115.4 <sup>a</sup> (-129.6) <sup>b</sup>
Mo(CO) <sub>5</sub> PH <sub>3</sub> <sup>g</sup>		-113.1	-113.1	-210.8	-13.3	-132.4	-145.7 <sup>a</sup> (-165.0) <sup>d</sup>
P(CH <sub>3</sub> ) <sub>3</sub> <sup>e</sup>	118.0 <sup>j</sup>	-83.1 (-60.8) <sup>s</sup>	-83.1 (-60.8) <sup>s</sup>	-45.1 (-68.4) <sup>s</sup>	1.3	-71.7	-70.4 <sup>a</sup> (-63.4) <sup>s</sup>
Cr(CO) <sub>5</sub> P(CH <sub>3</sub> ) <sub>3</sub> <sup>h</sup>		45.1	45.1	-45.1	7.2	7.8	15.0 <sup>a</sup> (6.5) <sup>i</sup>
Mo(CO) <sub>5</sub> P(CH <sub>3</sub> ) <sub>3</sub> <sup>n</sup>		6.1	6.1	-45.0	2.1	-13.0	-10.9 <sup>a</sup> (-17.0) <sup>d</sup>
PPh <sub>3</sub> <sup>f</sup>	145.0 <sup>j</sup>	1.9 (9.0) <sup>k</sup>	1.9 (9.0) <sup>k</sup>	-19.2 (-42.0) <sup>k</sup>	-1.8	-3.3	-5.1 <sup>a</sup> (-8.0) <sup>k</sup>
Cr(CO) <sub>5</sub> PPh <sub>3</sub> <sup>m</sup>		106.8 (127.0) <sup>k</sup>	94.2 (80.0) <sup>k</sup>	-7.4 (-42.0) <sup>k</sup>	1.4	63.1	64.5 <sup>a</sup> (55.0) <sup>k</sup>
Mo(CO) <sub>5</sub> PPh <sub>3</sub> <sup>o</sup>		85.5	71.1	-7.9	0.4	50.1	50.5 <sup>a</sup> (38.0) <sup>d</sup>
Cr(CO) <sub>4</sub> (CS)PPh <sub>3</sub> <sup>k</sup>		112.6 (101.0) <sup>k</sup>	106.9 (70.0) <sup>k</sup>	-20.2 (-37.0) <sup>k</sup>	1.1	65.3	66.4 <sup>a</sup> (46.0) <sup>k</sup>
PF <sub>3</sub> <sup>v</sup>	104.0 <sup>w</sup>	224.2 (166.0) <sup>s</sup>	224.2 (166.0) <sup>s</sup>	-39.4 (-15.0) <sup>s</sup>	10.4	125.9	136.3 <sup>a</sup> (105.7) <sup>s</sup>
Cr(CO) <sub>5</sub> PF <sub>3</sub> <sup>g</sup>		361.2	361.2	-117.3	10.4	191.4	201.7 <sup>a</sup> (174.0) <sup>z</sup>
Mo(CO) <sub>5</sub> PF <sub>3</sub> <sup>g</sup>		312.9	312.9	-97.1	10.7	165.5	176.2 <sup>a</sup> (147.0) <sup>d</sup>
PCl <sub>3</sub> <sup>u</sup>	124.0 <sup>w</sup>	320.4	320.4	168.4	-8.5	278.2	269.7 <sup>a</sup> (217.1) <sup>s</sup>
Cr(CO) <sub>5</sub> PCl <sub>3</sub> <sup>f</sup>		340.5	340.5	-44.3	-16.2	228.5	212.3 <sup>a</sup> (187.0) <sup>d</sup>
Mo(CO) <sub>5</sub> PCl <sub>3</sub> <sup>g</sup>		347.6	347.6	27.4	-16.0	256.9	240.9 <sup>a</sup> (152.4) <sup>s</sup>

<sup>a</sup> Calculated absolute chemical shielding  $\sigma_{\text{H}_3\text{PO}_4} = 315.5$  ppm,  $\sigma_{\text{H}_3\text{PO}_4}^d = 955.7$  ppm,  $\sigma_{\text{H}_3\text{PO}_4}^p = -640.2$  ppm; structural data from ref 34, (exptl value: <sup>31</sup>P in 85% H<sub>3</sub>PO<sub>4</sub> (aq)  $\sigma_{\text{H}_3\text{PO}_4} = 328.35$  ppm, ref 45), and  $\delta = \sigma_{\text{H}_3\text{PO}_4} - \sigma_{\text{substance}}$ ,  $\sigma^d = \sigma_{\text{H}_3\text{PO}_4}^d - \sigma_{\text{substance}}^d$ ,  $\delta^p = \sigma_{\text{H}_3\text{PO}_4}^p - \sigma_{\text{substance}}^p$ . <sup>b</sup> Reference 35. <sup>c</sup> Reference 10a. <sup>d</sup> Reference 1a. <sup>e</sup> Structural data from ref 36. <sup>f</sup> Structural data from ref 37. <sup>g</sup> Optimized structure. <sup>h</sup> Structural data from ref 38. <sup>i</sup> Reference 39. <sup>j</sup> Reference 33. <sup>k</sup> Reference 40. <sup>l</sup> Reference 41. <sup>m</sup> Reference 42. <sup>n</sup> Reference 43. <sup>o</sup> Reference 44. <sup>p</sup> Reference 47. <sup>q</sup> Optimized structure. <sup>r</sup> Experimental values in parentheses. The experimental data are reported with respect to <sup>31</sup>P in 85% H<sub>3</sub>PO<sub>4</sub> (aq). <sup>s</sup> Reference 45. Experimental data originally reported as absolute shieldings ( $\sigma$ ) were converted to chemical shifts ( $\delta$ ) using the experimental data <sup>31</sup>P in 85% H<sub>3</sub>PO<sub>4</sub> (aq)  $\sigma_{\text{H}_3\text{PO}_4} = 328.35$  ppm (ref 45) and  $\delta = \sigma_{\text{H}_3\text{PO}_4} - \sigma_{\text{substance}}$ . <sup>t</sup> Structural data from ref 43. <sup>u</sup> Structural data from ref 46. <sup>v</sup> Reference 37. <sup>w</sup> Reference 14. <sup>x</sup> Reference 15. <sup>y</sup> For all the systems except for M(CO)<sub>5</sub>PPh<sub>3</sub> and Cr(CO)<sub>4</sub>(CS)PPh<sub>3</sub>  $\delta_{xx}$  and  $\delta_{yy}$  are the perpendicular components,  $\delta_{\perp}$ , of the chemical shift tensor and  $\delta_{zz}$  is the parallel component,  $\delta_{\parallel}$ , of the chemical shift tensor. <sup>z</sup> Reference 48.

cases smaller in absolute terms, Table 1. The diamagnetic components will not contribute much to the chemical shift (relative to H<sub>3</sub>PO<sub>4</sub>)

$$\delta = \sigma_{\text{H}_3\text{PO}_4} - \sigma_{\text{compound}} = \delta^d + \delta^p \quad (5)$$

since the diamagnetic shielding largely comes from constant core terms that are the same in all phosphorus compound and thus cancel out in the expression for the diamagnetic shift

$$\delta^d = \sigma_{\text{H}_3\text{PO}_4}^d - \sigma_{\text{compound}}^d \quad (6)$$

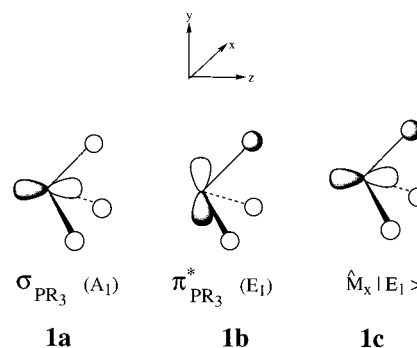
The chemical shift is instead dominated by the paramagnetic contribution

$$\delta^p = \sigma_{\text{H}_3\text{PO}_4}^p - \sigma_{\text{compound}}^p \quad (7)$$

as the paramagnetic shielding  $\sigma^p$  varies considerable among phosphorus compound, Table 1. The calculated chemical shifts for the free PR<sub>3</sub> molecules are given in Table 2.

The leading paramagnetic contribution to  $\sigma_{\perp}^p$  (Table 1) comes from the coupling between the occupied  $\sigma_{\text{PR}_3}$  HOMO, **1a**, and the virtual  $\pi_{\text{PR}_3}^*$  orbitals, **1b**, of PR<sub>3</sub> through the matrix elements  $\langle \sigma_{\text{PR}_3} | \hat{M}_s | \pi_{\text{PR}_3}^* \rangle$  ( $s = x$  or  $y$ )<sup>31</sup>. The function  $\hat{M}_x | \pi_{\text{PR}_3}^* \rangle$ , **1c**<sup>32</sup>, will have the form of a  $\sigma$ -type orbital, and thus

overlap with the HOMO **1a**. The same type of coupling is found in the case of free CO<sup>10a</sup> between  $\sigma_{\text{CO}}$  and  $\pi_{\text{CO}}^*$ .



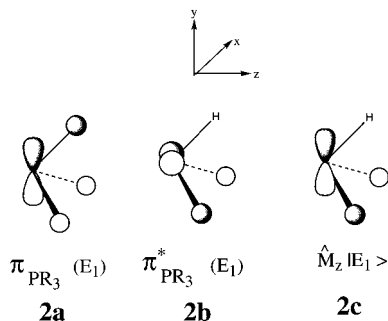
The paramagnetic shielding component  $\sigma_{\perp}^p$  is inversely proportional to the gap between occupied and virtual orbitals, eq 3. The orbital energies of the occupied  $\sigma_{\text{PR}_3}$  orbitals and the virtual  $\pi_{\text{PR}_3}^*$  orbitals are reported in Table 3 along with the energy gap. It is observed from Tables 1 and 3 that, in general, without considering PF<sub>3</sub>, the smaller the energy gap the larger the paramagnetic shielding  $\sigma_{\perp}^p$  components in absolute terms  $|\sigma_{\perp}^p|$ . PCl<sub>3</sub> presents the smallest energy gap and the largest value for  $|\sigma_{\perp}^p|$ . PF<sub>3</sub> has the largest energy gap but it does present the smallest value for  $|\sigma_{\perp}^p|$  as expected. In this case

**TABLE 3: Orbital Energies for the  $\sigma_{PR_3}$ ,  $\pi_{PR_3}$ , and  $\pi^*_{PR_3}$ -Type Orbitals and Energy Gaps between  $\sigma$  and  $\pi^*$  and  $\pi$  and  $\pi^*$  Orbitals for the Free Phosphines**

system	orbital energy (eV)			energy gap between $\sigma$ and $\pi^*$ orbitals (eV)	energy gap between $\pi$ and $\pi^*$ orbitals (eV)
	$\pi$ -type orbital	$\sigma$ -type orbital	$\pi^*$ -type orbital		
PH <sub>3</sub>	-9.603	-6.812	-0.365	6.447	9.238
P(CH <sub>3</sub> ) <sub>3</sub>	-7.904	-5.000	0.615	5.615	8.519
PPh <sub>3</sub>	-8.259	-5.571	0.308	5.879	8.567
PF <sub>3</sub>	-14.349	-8.244	-1.676	6.568	12.673
PCl <sub>3</sub>	-11.795	-7.288	-2.419	4.869	9.376

other factors defining  $\sigma_{\perp}^p$  such as the magnitude of the matrix elements  $\langle \Psi_a | \hat{M}_u | \Psi_i \rangle$ , eq 3, and the  $r_N^{-3}$  factor in the integrant of eq 1 become important as well. There is a good agreement between theory and experiment for the perpendicular shielding component  $\sigma_{\perp}$  in the case of PH<sub>3</sub>, P(CH<sub>3</sub>)<sub>3</sub>, and P(C<sub>6</sub>H<sub>5</sub>)<sub>3</sub>. The error in  $\sigma_{\perp}$  is much larger for PF<sub>3</sub>. We attribute the error for PF<sub>3</sub> and PCl<sub>3</sub> to an overestimation of  $|\sigma_{\perp}^p|$ .

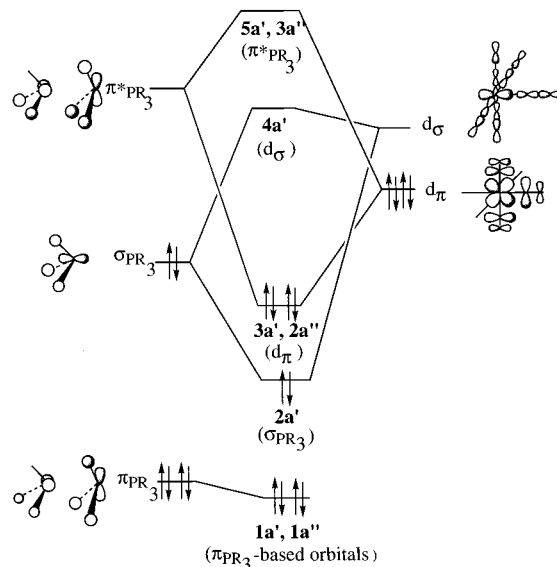
The parallel paramagnetic shielding component  $\sigma_{\parallel}^p$  comes from the coupling between the occupied  $\pi_{PR_3}$  orbitals, **2a**, and  $\pi^*_{PR_3}$ , **2b**, through the common lobes in  $\hat{M}_z |\pi^*_{PR_3}\rangle$ . For the case of free CO the paramagnetic contribution  $\sigma_{\parallel}^p$  is zero. This is due to the fact that  $\langle \pi_{yCO} | \hat{M}_z | \pi^*_{xCO} \rangle = 0$  because  $\hat{M}_z |\pi^*_{xCO}\rangle$  happens to be equal to  $\pi^*_{yCO}$  and  $\langle \pi_{yCO} | \pi^*_{yCO} \rangle = 0$ .



**TABLE 4: Paramagnetic Contributions to the Calculated <sup>31</sup>P Coordination Shift<sup>a</sup> in M(CO)<sub>5</sub>PR<sub>3</sub>**

system	$\Delta\delta^{p_{xx}}$ (ppm) <sup>c</sup>	$\Delta\delta^{p_{yy}}$ (ppm) <sup>c</sup>	$\Delta\delta^{p_{zz}}$ (ppm) <sup>c</sup>	$\Delta\delta^b$ (exptl) (ppm) <sup>a</sup>
Cr(CO) <sub>5</sub> PH <sub>3</sub>	211.1	211.1	5.86	139.3 (136.5)
Cr(CO) <sub>5</sub> P(CH <sub>3</sub> ) <sub>3</sub>	118.2	118.2	2.2	85.5 (69.9)
Cr(CO) <sub>5</sub> PPh <sub>3</sub>	100.3	88.1	10.7	69.6 (63.0)
Cr(CO) <sub>5</sub> PF <sub>3</sub>	134.7	134.7	-73.0	65.4 (68.3)
Cr(CO) <sub>5</sub> PCl <sub>3</sub>	25.4	25.4	-199.9	-57.4 (-30.1)
Mo(CO) <sub>5</sub> PH <sub>3</sub>	167.0	167.0	5.6	109.0 (101.1)
Mo(CO) <sub>5</sub> P(CH <sub>3</sub> ) <sub>3</sub>	83.6	83.6	9.0	59.5 (46.4)
Mo(CO) <sub>5</sub> PPh <sub>3</sub>	82.7	65.7	11.7	55.7 (46.0)
Mo(CO) <sub>5</sub> PF <sub>3</sub>	86.7	86.7	-54.7	31.2 (41.3)
Mo(CO) <sub>5</sub> PCl <sub>3</sub>	32.5	32.5	-128.9	-28.8 (-64.7)

<sup>a</sup> Coordination shift:  $\Delta\delta = \sigma_{PR_3} - \sigma_{[M(CO)_5PR_3]}$ . <sup>b</sup>  $\Delta\delta = \sum_{s=1}^3 \Delta\delta_{ss}^p + \Delta\delta^d$ . <sup>c</sup>  $\Delta\delta_{ss}^p = \sigma_{ss,PR_3}^p - \sigma_{ss,[M(CO)_5PR_3]}^p$  is the difference in the paramagnetic shielding between  $[M(CO)_5PR_3]$ ,  $\sigma_{ss,[M(CO)_5PR_3]}^p$  and the ligand PR<sub>3</sub>,  $\sigma_{ss,PR_3}^p$ .



**Figure 2.** Schematic orbital interaction diagram for M(CO)<sub>5</sub>PR<sub>3</sub>.

Experimental shift tensor components have been reported for Cr(CO)<sub>5</sub>PPh<sub>3</sub> and Cr(CO)<sub>4</sub>(CS)PPh<sub>3</sub>, Table 2. It is gratifying to note that the GIAO-DFT method affords  $\delta_{ss}$  ( $ss = xx, yy, zz$ ) values in reasonable agreement with experiment for these rather large systems, Table 2. We note that the  $\delta_{xx}$  and  $\delta_{yy}$  components perpendicular to P–M bond vector differ considerably from the corresponding  $\delta_{xx}$  and  $\delta_{yy}$  components of the free PPh<sub>3</sub> ligand perpendicular to the C<sub>3</sub>-axis. On the other hand the  $\delta_{zz}$  component along the M–P bond vector is quite similar to the  $\delta_{zz}$  component along the C<sub>3</sub>-axis in the free PPh<sub>3</sub> ligand. We shall now turn to an interpretation of the observed changes in the <sup>31</sup>P chemical shift as PR<sub>3</sub> is complexed to the metal center,  $\Delta\delta$  of eq 4. The calculated and experimental values of  $\Delta\delta$  for the M(CO)<sub>5</sub>PR<sub>3</sub> systems are tabulated in Table 4. A schematic orbital interaction diagram for M(CO)<sub>5</sub>PR<sub>3</sub> is given in Figure 2. The diagram presents the key orbitals of M(CO)<sub>5</sub>PR<sub>3</sub> resulting from the interaction of  $\sigma_{PR_3}$ ,  $\pi_{PR_3}$ , and  $\pi^*_{PR_3}$  of PR<sub>3</sub> with  $d_{\sigma}$  and  $d_{\pi}$  of the M(CO)<sub>5</sub> fragment.

The all-dominating paramagnetic part,  $\Delta\delta^p$ , of the coordination shift,  $\Delta\delta$ , has contributions from the coupling between occupied and virtual orbitals  $\Delta\delta^{oc-vir}$ , as well as contributions  $\Delta\delta^{oc}$  that only depend on the occupied orbitals. Our calculations show that the trends in  $\Delta\delta$  between different phosphine complexes, Table 4, correlates with the paramagnetic coupling between occupied and virtual orbitals  $\Delta\delta^{oc-vir}$ . We have, in order to gain further insight into the coordination chemical shift,

The energy gap between  $\pi^*_{PR_3}$  and  $\pi_{PR_3}$  is smaller in PMe<sub>3</sub> and P(C<sub>6</sub>H<sub>5</sub>)<sub>3</sub> than in PH<sub>3</sub>, Table 3, this produces a numerically larger paramagnetic  $\sigma_{\parallel}^p$  shielding in PMe<sub>3</sub> and P(C<sub>6</sub>H<sub>5</sub>)<sub>3</sub> compared to PH<sub>3</sub>, Table 1. For the PX<sub>3</sub> systems  $\sigma_{\parallel}^p$  is numerically large in the case of PF<sub>3</sub> although it has the biggest energy gap, Table 3. Again, other factors seems to be dominating for this molecule.

Kaup<sup>6f</sup> found from a set of SOS-DFPT calculations that the most important contributions to the <sup>31</sup>P chemical shift of free PR<sub>3</sub> are due to paramagnetic couplings between the occupied P–R bonding orbitals **1a,b** and the lowest-lying virtual orbital **1c** in accordance with our findings. Kaupp used a correction<sup>5b,30</sup> to the orbital energy gap of eq 3 which affords somewhat better results for PF<sub>3</sub> and PCl<sub>3</sub>. The foundation of this correction is not yet clear<sup>8a,c</sup> and it has not been applied here.

**5. General Considerations for M(CO)<sub>5</sub>PR<sub>3</sub> Systems**

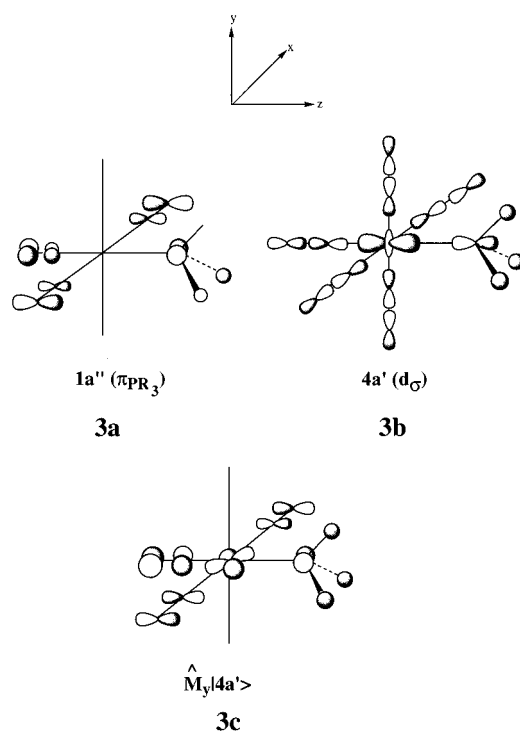
It follows from Table 2 that the calculated <sup>31</sup>P chemical shifts for the phosphine substituted metal carbonyls are in good agreement with the experimental values. The theoretical estimates are derived from a single “frozen” molecule in the gas phase at 0 K without corrections for thermal motions and solvent effects. It follows further from Table 2 that it is the paramagnetic contribution to the chemical shift  $\delta^p$  that determines the total value of  $\delta$  in the phosphine-substituted metal carbonyls, whereas the diamagnetic  $\delta^d$  term is numerically small.

displayed the individual components  $\Delta\delta_{ss}^p$  ( $s = x, y,$  and  $z$ ) of  $\Delta\delta^p$  in Table 4.

The distortion of the  $\text{PR}_3$  ligand on complexation has a positive contribution ( $<20$  ppm) to  $\Delta\delta_{ss}^p$  ( $s = x, y,$  and  $z$ ). We have previously found<sup>10a</sup> that the CO bond stretch in  $\text{M}(\text{CO})_6$  has an important contribution to  $\Delta\delta_{ss}^p$  (around 10 ppm in  $^{13}\text{C}$  NMR and around 20 ppm in  $^{17}\text{O}$  NMR).

### 6. $^{31}\text{P}$ Coordination Shifts in $\text{M}(\text{CO})_5\text{PH}_3$ , $\text{M}(\text{CO})_5\text{PMe}_3$ , and $\text{M}(\text{CO})_5\text{PPh}_3$

For these systems, our calculations reveal that the two components  $\Delta\delta_{xx}^p$  and  $\Delta\delta_{yy}^p$  are determined principally by the paramagnetic coupling the occupied  $\pi_{\text{PR}_3}$ -based orbitals  $1a''$ - $1a''$  and the virtual  $d_\sigma$ -type orbital  $4a'$ , Figure 2. The occupied  $\pi_{\text{PR}_3}$ -type orbital  $1a''$ , **3a**, interacts with the virtual  $d_\sigma$ -type orbital  $4a'$ , **3b**, through the common lobes in  $\hat{M}_y|4a'\rangle$ , **3c**. Similar interactions can be found for the  $x$ -direction involving  $\hat{M}_x$ .



The coupling in **3c** represents a (negative) paramagnetic contribution to the  $^{31}\text{P}$  shielding in the  $\text{M}(\text{CO})_5\text{PR}_3$  complex not present (possible) in the free  $\text{PR}_3$  ligand. It will as a consequence afford a positive contribution to  $\Delta\delta$ , eq 4. The positive contribution from **3c** to  $\Delta\delta$  should to a first approximation be inversely proportional to the energy gap between the  $1a''$  and  $4a'$  orbitals, eq 3. We find indeed that a decrease in the energy gap along  $\text{M}(\text{CO})_5\text{PH}_3 < \text{M}(\text{CO})_5\text{PMe}_3 < \text{M}(\text{CO})_5\text{PPh}_3$ , Table 5, gives rise to an increase in  $\Delta\delta$  following the order  $\text{M}(\text{CO})_5\text{PH}_3 > \text{M}(\text{CO})_5\text{PMe}_3 > \text{M}(\text{CO})_5\text{PPh}_3$  for both metals, Table 4.

We note that the energy of the virtual  $d_\sigma$ -type orbital  $4a'$ , **3b**, is lower, Table 5, for  $\text{M}(\text{CO})_5\text{PH}_3$  than the energies for  $\text{M}(\text{CO})_5\text{PMe}_3$  and  $\text{M}(\text{CO})_5\text{PPh}_3$ . The lower energy is in part responsible for the smaller energy gap between  $1a''$  and  $4a'$  which leads to a larger coordination shift. The low energy of  $4a'$ , **3b**, in  $\text{M}(\text{CO})_5\text{PH}_3$  reflects the fact that  $\text{PH}_3$  is a poor  $\sigma$ -donor with a  $\sigma_{\text{PR}_3}$  orbital of low energy, Table 3. The low energy of  $\sigma_{\text{PH}_3}$  will lead to a weak interaction with  $d_\sigma$  of  $\text{M}(\text{CO})_5$ , Figure 2, and a modest destabilization of  $4a'$ , **3b**, which is an out-of-

**TABLE 5: Energy Gaps  $\Delta E$  between  $1a''$  and  $4a'$  in  $\text{M}(\text{CO})_5\text{PR}_3$**

system	energy (eV) $\pi_{\text{PR}_3}$ -type $1a''$	energy (eV) $d_\sigma$ -type $4a'$	$\Delta E$ (eV)
$\text{Cr}(\text{CO})_5\text{PH}_3$	-10.690	-0.553	10.137
$\text{Cr}(\text{CO})_5\text{P}(\text{CH}_3)_3$	-9.000	1.409	10.409
$\text{Cr}(\text{CO})_5\text{PPh}_3$	-8.903	3.045	11.948
$\text{Cr}(\text{CO})_5\text{PF}_3$	-14.766	2.163	12.603
$\text{Cr}(\text{CO})_5\text{PCl}_3$	-12.329	-1.192	12.137
$\text{Mo}(\text{CO})_5\text{PH}_3$	-10.696	-0.281	10.415
$\text{Mo}(\text{CO})_5\text{P}(\text{CH}_3)_3$	-9.067	2.107	11.174
$\text{Mo}(\text{CO})_5\text{PPh}_3$	-8.814	3.257	12.071
$\text{Mo}(\text{CO})_5\text{PF}_3$	-14.903	-1.045	13.858
$\text{Mo}(\text{CO})_5\text{PCl}_3$	-12.108	-0.768	11.340

**TABLE 6: Population in the  $\pi^*$ -Type Orbitals for  $\text{M}(\text{CO})_5\text{PR}_3$  Complexes**

system	total population in the two $\pi^*_{\text{PR}_3}$ orbitals
$\text{Cr}(\text{CO})_5\text{PH}_3$	0.126
$\text{Cr}(\text{CO})_5\text{P}(\text{CH}_3)_3$	0.120
$\text{Cr}(\text{CO})_5\text{PPh}_3$	0.082
$\text{Cr}(\text{CO})_5\text{PF}_3$	0.326
$\text{Cr}(\text{CO})_5\text{PCl}_3$	0.374
$\text{Mo}(\text{CO})_5\text{PH}_3$	0.168
$\text{Mo}(\text{CO})_5\text{P}(\text{CH}_3)_3$	0.030
$\text{Mo}(\text{CO})_5\text{PPh}_3$	0.064
$\text{Mo}(\text{CO})_5\text{PF}_3$	0.260
$\text{Mo}(\text{CO})_5\text{PCl}_3$	0.310

phase combination between  $\sigma_{\text{PH}_3}$  and  $d_\sigma$ . Our analysis would indicate that the observed  $^{31}\text{P}$  coordination shift components  $\Delta\delta_{ss}$  ( $s = x$  or  $y$ ) for  $\text{M}(\text{CO})_5\text{PR}_3$  and related alkyl or phenyl phosphine complexes can be taken as a measure for the degree of donation from  $\sigma_{\text{PR}_3}$  to  $d_\sigma$  with the poorest donors affording the largest values for  $\Delta\delta_{ss}$  ( $s = x$  or  $y$ ).

There is a clear reduction in the  $^{31}\text{P}$  coordination shift for a given  $\text{PR}_3$  ligand as we move from chromium to molybdenum, Table 4. The  $d_\sigma$  orbital of the 4d element forms stronger overlaps<sup>49</sup> with  $\sigma_{\text{PR}_3}$  leading to the higher energy of  $4a'$ , Table 5, and the smaller coordination shift components  $\Delta\delta_{ss}$  ( $s = x, y$ ), Table 4.

The third coordination shift component  $\Delta\delta_{zz}$  is very small, Table 4, for  $\text{M}(\text{CO})_5\text{PH}_3$ ,  $\text{M}(\text{CO})_5\text{PMe}_3$ , and  $\text{M}(\text{CO})_5\text{PPh}_3$ , will not be discussed any further here. We note further that the interaction between  $d_\pi$  of  $\text{M}(\text{CO})_5$  and  $\pi^*_{\text{PR}_3}$  of the  $\text{PR}_3$  ligand, Figure 2, is relatively weak for  $\text{PH}_3$ ,  $\text{P}(\text{CH}_3)_3$ , and  $\text{PPh}_3$  due to the high energy of  $\pi^*_{\text{PR}_3}$ , Table 3. There is as a consequence very little back-donation from  $d_\pi$  to  $\pi^*_{\text{PR}_3}$ , as illustrated in Table 6.

### 7. $^{31}\text{P}$ Coordination Shifts in $\text{M}(\text{CO})_5\text{PF}_3$ and $\text{M}(\text{CO})_5\text{PCl}_3$

The coordination shifts for  $\text{M}(\text{CO})_5\text{PF}_3$  and  $\text{M}(\text{CO})_5\text{PCl}_3$  are a bit more complex as already noted by Kaupp.<sup>6f</sup> However, we shall demonstrate that they can be interpreted as well in relatively simple terms.

The  $\text{PF}_3$  and  $\text{PCl}_3$  ligands have low-lying  $\pi^*_{\text{PX}_3}$  orbitals, Table 3, that can interact with  $d_\pi$  leading to a back-donation of charge from  $d_\pi$  to  $\pi^*_{\text{PX}_3}$  that is much larger than in the case of the  $\text{PH}_3$ ,  $\text{PMe}_3$ , and  $\text{PPh}_3$  ligands, Table 6. A result of this interaction is a destabilization of  $\pi^*_{\text{PX}_3}$  as the major component in the  $3a''$ ,  $5a'$  orbitals, Figure 2, both of which are out-of-phase combinations between  $d_\pi$  and  $\pi^*_{\text{PX}_3}$ . The back-donation will reduce the  $\sigma_{\text{PX}_3}$  to  $\pi^*_{\text{PX}_3}$  paramagnetic couplings, **1c**, in the  $x$  and  $y$  directions and the  $\pi_{\text{XP}_3}$  to  $\pi^*_{\text{PX}_3}$  paramagnetic coupling in the  $z$ -direction for the complexed  $\text{PX}_3$  ligand compared to free  $\text{PX}_3$  since the  $\pi^*_{\text{PX}_3}$  energy effectively has been raised in

the complex as a result of the back-donation, Figure 2. The result is negative contributions to  $\Delta\delta_{ss}$  ( $s = x, y$ ) and  $\Delta\delta_{zz}$ . The negative contributions to  $\Delta\delta_{ss}$  ( $s = x, y$ ) and  $\Delta\delta_{zz}$  are further compounded by stabilizations of  $\sigma_{PX_3}$  (2a') and  $\pi_{PX_3}$  (1a', 1a'') in coordinated  $PX_3$ , Figure 2, which add to the energy gap between the occupied and virtual orbitals.

It follows from Table 4 that the total coordination shift component  $\Delta\delta_{zz}$  is negative and we attribute this to the above mentioned reduction of the  $\pi_{PX_3}$  to  $\pi^*_{PX_3}$  paramagnetic coupling in the  $M(CO)_5PF_3$ ,  $M(CO)_5PCl_3$  complexes. We note in this regard that the better  $\pi$ -acceptor  $PCl_3$ , Table 6, has the more negative  $\Delta\delta_{zz}$  component, Table 4. Our analysis would suggest that  $\Delta\delta_{zz}$  in experimental studies could be used as an indicator for the degree of back-donation. The total  $\Delta\delta_{ss}$  ( $s = x, y$ ) components in Table 4 are positive as the paramagnetic coupling, **3c**, between the occupied  $\pi_{PR_3}$ -type orbitals 1a', 1a'', **3a**, and the virtual  $d_\sigma$ -type orbital 4a', **3b**, add a positive contribution to  $\Delta\delta_{ss}$  ( $s = x, y$ ) as in the case of the  $PH_3$ ,  $PMe_3$ , and  $PPh_3$  ligands. However, it is diminished by the negative contribution from the reduction in the coupling between  $\sigma_{PX_3}$  and  $\pi^*_{PX_3}$  for complexed  $PR_3$ . Especially  $PCl_3$  with the strongest back-donation, Table 6, is seen to have the smallest  $\Delta\delta_{ss}$  ( $s = x, y$ ) component of all the ligands, Table 4.

The finding here that  $PCl_3$  is a better  $\pi$ -acceptor than either of the other ligands considered, including  $PF_3$ , is in agreement with conclusions drawn from IR spectroscopy,<sup>50a</sup> metal-phosphorus NMR coupling constants,<sup>50b</sup> as well as M–P bond distances. There has been some discussion<sup>15</sup> in the literature about whether the observed <sup>31</sup>P coordination shift also support this notion. However, our analysis shows that the negative coordination shift for  $PCl_3$  in fact is a consequence of the  $\pi$ -acceptor ability of this ligand.

It is well established<sup>51</sup> that the  $\pi$ -acceptor ability for CX ( $X = O, S, Se, \text{ and } Te$ ) increases from oxygen to tellurium. This can be explained by observing that similar overlaps between orbitals on carbon and X will decrease from  $X = O$  to  $X = Te$ . The decrease in overlap will in turn make  $\pi^*_{CX}$  less anti-bonding and more stable for the higher homologous. Similar arguments holds for P–X overlaps and the energy of  $\pi^*_{PX_3}$  ( $X = F$  and  $Cl$ ), Table 3. In fact, the  $\pi$ -acceptor ability should increase from  $X = F$  to  $X = I$  as  $\pi^*_{PX_3}$  becomes increasingly stable. It is interesting to note that the coordination chemical shift in accordance with the arguments given above becomes increasingly negative<sup>1</sup> from  $X = F$  to  $X = I$ . Unfortunately, we are at the moment not able to calculate the chemical shift  $s$  of  $PX_3$  for  $X = Br$  and  $I$  since a proper relativistic treatment including spin-orbit is required.

### 8. <sup>95</sup>Mo NMR

The calculated and experimental <sup>95</sup>Mo chemical shift for  $Mo(CO)_5PPh_3$ ,  $Mo(CO)_5PF_3$  and  $Mo(CO)_5PCl_3$  are presented in Table 7. Our calculations clearly reproduce the observed trend in the chemical shift as  $Mo(CO)_5PPh_3 < Mo(CO)_5PF_3 \ll Mo(CO)_5PCl_3$ .

The trend in the <sup>95</sup>Mo chemical shift is determined by the paramagnetic shielding component  $\sigma^p$  with the largest contribution  $\sigma^{occ-vir}$  originating from the coupling between the  $d_\pi$  HOMO and the  $d_\sigma$  LUMO, Figure 2. Both  $\sigma^p$  and  $\sigma^{occ-vir}$ , as well as the energies of  $d_\pi$  and  $d_\sigma$ , are given in Table 8.

$Mo(CO)_5PPh_3$  has the largest energy gap, 6.226 eV, and the smallest, in absolute terms, paramagnetic shielding, –2606.8 ppm. On the other hand,  $Mo(CO)_5PCl_3$  presents the smallest energy gap 5.820 eV and the largest paramagnetic shielding, –3041.2 ppm, Table 8. We do not feel that the <sup>95</sup>Mo chemical

**TABLE 7. Calculated and Experimental <sup>95</sup>Mo Chemical Shift Tensor Components (ppm) and Isotropic Chemical Shift for Several Phosphine-Substituted Metal Carbonyls**

system	$\delta_{xx}$	$\delta_{yy}$	$\delta_{zz}$	$\delta^d$	$\delta^p$	chemical shift $\delta$ (exptl) <sup>a</sup>
$Mo(CO)_5PPh_3$ <sup>b</sup>	–1668.6	–1662.1	–1837.3	4.4	–1727.1	–1722.7 (–1743.0) <sup>c</sup>
$Mo(CO)_5PF_3$ <sup>d</sup>	–1760.2	–1745.4	–1753.1	6.1	–1759.0	–1752.9 <sup>e</sup> (–1860.0) <sup>c</sup>
$Mo(CO)_5PCl_3$ <sup>f</sup>	–1196.8	–1179.6	–1555.6	–2.6	–1308.0	–1310.6 (–1523.0) <sup>c</sup>

<sup>a</sup> Experimental data reported with respect to  $[MoO_4]^{2-}$ . <sup>b</sup> Reference 43. <sup>c</sup> Reference 15. <sup>d</sup> Reference 47. <sup>e</sup> Calculated absolute chemical shielding  $\sigma_{[MoO_4]^{2-}} = -374.0$  ppm,  $\sigma_{[MoO_4]^{2-}}^d = 3992$  ppm, and  $\sigma_{[MoO_4]^{2-}}^p = -4366$  ppm.  $\delta = \sigma_{[MoO_4]^{2-}} - \sigma_{substance}$ ,  $\delta^d = \sigma_{[MoO_4]^{2-}}^d - \sigma_{substance}^d$ , and  $\delta^p = \sigma_{[MoO_4]^{2-}}^p - \sigma_{substance}^p$ . <sup>f</sup> Optimized structure.

**TABLE 8. Paramagnetic Shielding in <sup>95</sup>Mo NMR for Several Phosphine-Substituted Metal Carbonyls**

system	total paramagnetic shielding $\sigma^p$ (ppm)	$\sigma^{occ-vir}$ (ppm)	energy of $d_\pi$ orbital (eV)	energy of $d_\sigma$ orbital (eV)	energy gap (eV)
$Mo(CO)_5PPh_3$	–2638.9	–2606.8	–5.961	0.265	6.226
$Mo(CO)_5PF_3$	–2607.0	–2612.4	–7.011	–1.045	5.966
$Mo(CO)_5PCl_3$	–3057.9	–3041.4	–6.585	–0.768	5.820

shift can be used as an indication of  $\sigma$ -donation of  $\pi$ -back-donation as either type of bonding could increase the energy gap between  $d_\pi$  and  $d_\sigma$ .

### 9. Conclusions

We have studied the <sup>31</sup>P coordination shift  $\Delta\delta$  for the phosphine-substituted metal carbonyls  $M(CO)_5PR_3$  ( $M = Cr$  and  $Mo$ ;  $PR_3 = PH_3, PMe_3, \text{ and } PPh_3$ ),  $Cr(CO)_4CSPH_3$ , and  $M(CO)_5PX_3$  ( $X = F$  and  $Cl$ ) as well as the <sup>95</sup>Mo NMR chemical shift in  $Mo(CO)_5PPh_3$  and  $Mo(CO)_5PX_3$  ( $X = F$  and  $Cl$ ). This is the first theoretical NMR study on phosphine complexes that includes  $PPh_3$  as a ligand and compares calculated and experimental shift components  $\Delta\delta_{ss}$  ( $s = x, y, \text{ or } z$ ). Calculations on <sup>95</sup>Mo NMR for phosphine complexes have not previously been reported.

For  $M(CO)_5PR_3$  ( $M = Cr$  and  $Mo$ ;  $PR_3 = PH_3, PMe_3, \text{ and } PPh_3$ ) the dominating contribution,  $\Delta\delta_{xx}^p + \Delta\delta_{yy}^p$ , to the coordination shift comes from the paramagnetic coupling between the occupied  $\pi_{PR_3}$ -type orbitals and the virtual  $d_\sigma$  orbitals, **3c**. It is suggested that the  $xx, yy$  components of the coordination shift can be used as an indicator for the donor ability of alkyl and phenyl phosphines, with a large component corresponding to a relatively weak donor.

Our calculations indicate that  $PF_3$  and (especially)  $PCl_3$  are much better  $\pi$ -acceptors than  $PH_3, PMe_3, \text{ and } PPh_3$ , in agreement with the findings from numerous previous investigations. We have shown that back-donation will reduce the  $\sigma_{PX_3}$  to  $\pi^*_{PX_3}$  paramagnetic couplings, **1c**, in the  $x, y$  directions and the  $\pi_{PX_3}$  to  $\pi^*_{PX_3}$  paramagnetic coupling in the  $z$ -direction, **2c**, for the complexed  $PX_3$  ligand compared to free  $PX_3$  since the  $\pi^*_{PX_3}$  energy effectively has been raised in the complex as a result of the back-donation. The result is negative contributions to  $\Delta\delta_{ss}$  ( $s = x$  or  $y$ ) and  $\Delta\delta_{zz}$  in addition to the positive contribution from **3c** to  $\Delta\delta_{xx}^p + \Delta\delta_{yy}^p$ . The back-donation renders the  $\Delta\delta_{zz}$  component of  $PX_3$  complexes negative and the total coordination shift for the better  $\pi$ -acceptor  $PCl_3$  negative. This is the first interpretation of the complex patterns in the coordination shift of  $PX_3$  ligands, based on quantitative calculations.

**Acknowledgment.** This work has been supported by the National Sciences and Engineering Research Council of Canada (NSERC). Y.R.-M. acknowledges a scholarship from DGAPA-UNAM (Mexico), and T. Z. acknowledges a Canada Council Killam Research Fellowship. We thank the Petroleum Research Fund administered by the American Chemical Society (ACS-PRF Grant 31205-AC3) for further support of this research.

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- (31) The bracket notation  $\langle \Psi_1 | \hat{M}_x | \Psi_2 \rangle$  denotes certain matrix elements (integrals) between the two orbitals  $\Psi_1$  and  $\Psi_2$  that contribute to the paramagnetic shielding  $\sigma^p$ .
- (32) The expression  $|\hat{M}_x | \pi_{PR}^* \rangle$  denotes an orbital resulting from the action of the operator  $\hat{M}_x$  on the  $\pi_{PR}^*$  orbital.
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